Discuss the following problems with the people at your table.

1. Let P(x) be the predicate "x is an ash tree" and let Q(x) be the predicate "x is vulnerable to the emerald ash borer."

Consider the sentence:

Every ash tree is vulnerable to the emerald ash borer.

- (a) Rewrite the sentence above as a universal conditional statement using the symbols P(x) and Q(x).
- (b) What is the negation of your universal conditional statement in part (a)?
- (c) What is the *contrapositive* of your universal conditional statement in part (a)?
- (d) What is the *converse* of your universal conditional statement in part (a)?
- (e) What is the *inverse* of your universal conditional statement in part (a)?
- 2. Write the following statements in formal logic notation, being sure to specify all of the predicate symbols that you use. Then write the negation of each statement, both in English and using formal logic symbols.
 - (a) If a polygon is a triangle, then its interior angles sum to 2π radians.
 - (b) If a polygon has interior angles that sum to 2π radians, then it is a triangle.

3.	Determine whether each statement is true or false.	
	(a) Every hunk of iron that floats in water is a hunk of gold.	ਹੈ Are you sure?
	(b) There is a hunk of iron that floats in water, which is not a hunk of gold.	
	(c) Every number that is both even and odd is a multiple of 6.	
	(d) There is a number that is both even and odd, which is not a multiple of 6.	
4.	Decide whether each statement is true or false. Then write the statement in formal logic symbols, specifying all predicate symbols that you use. Lastly, negate each statement.	
	(a) To earn an A in this class, it is necessary to be enrolled in this class.	
	(b) To earn an A in this class, it is sufficient to be enrolled in this class.	

5.	Consider the following statement:				
		There exists a student who has taken every course at St. Olaf College.			
	(a)	Express the statement above using logical symbols, defining each predicate symbol that you use.	ூ How many quantifiers do you need?		
	(b)	What is the negation of the statement above?			
6.		multiplicative inverse of a real number x is a real number y such that $xy = 1$. Consider the wing statement:			
		Every real number has a multiplicative inverse.			
	(a)	Express the statement above using logical symbols, defining each predicate symbol that you use. $ \\$			
	(b)	What is the negation of the statement above?			
	(c)	Which is true, the original statement or its negation?			