

## Optimization problem from last time

MAXIMIZE:  $n_0 \cdot n_1 \cdot n_2 \cdots n_q$

MINIMIZE:  $-n_0 \cdot n_1 \cdot n_2 \cdots n_q$

or  $-\ln(n_0 \cdot n_1 \cdot n_2 \cdots n_q + 1)$

recall:

$df = \text{diff. in}$   
func. values

compute:

$$e^{-df/k}$$

## MAGIC SQUARE:

An  $n \times n$  grid filled with the integers  $1, 2, 3, \dots, n^2$  such that all row, column, and diagonal sums are the same.

not a magic square:

1	7	6	14
8	5	3	16
4	2	9	15
15	13	14	18
			16

sum of  $k$  consecutive integers:

$$\begin{array}{r}
 1 + 2 + 3 + \dots + (k-1) + k = \frac{1}{2}k(k+1) \\
 + k + (k-1) + (k-2) + \dots + 2 + 1 \\
 \hline
 (k+1) + (k+1) + (k+1) + \dots + (k+1) + (k+1) \leftarrow k \text{ pairs}
 \end{array}$$

So the sum is  $k(k+1)$

let  $k = n^2$ :

$$1 + 2 + 3 + \dots + n^2 = \frac{1}{2} n^2 (n^2 + 1)$$

sum of all  
 $n^2$  numbers  
in the magic  
square

If we have a magic square, then each row, column, and diagonal must add up to:

$$\frac{1}{n} \left( \frac{1}{2} n^2 (n^2 + 1) \right) = \frac{1}{2} n (n^2 + 1)$$

If  $n=3$ : sums are  $\frac{1}{2} (3)(3^2+1) = \frac{1}{2} (3)(10) = 15$ .

Using simulated annealing to find magic squares:

1. What are the states?
2. How do we move between states?
3. What function do we minimize?