

Collatz Function:

$$c(n) = \begin{cases} 3n+1 & \text{if } n \text{ is odd} \\ \frac{n}{2} & \text{if } n \text{ is even} \end{cases}$$

Iterate  $c(n)$  for various starting values  $n$ .  
What patterns emerge?

$n=5$ :

$$c(5) = 3(5) + 1 = 16$$

$$c(16) = \frac{16}{2} = 8$$

$$c(8) = 4$$

$$c(4) = 2$$

$$c(2) = 1$$

$$c(1) = 3(1) + 1 = 4$$

cycle: 4, 2, 1, 4, 2, 1, ...

Collatz Conjecture: Starting with any positive integer  $n$ , the sequence of Collatz iterates eventually reaches 1.

This has been computationally verified up to about  $10^{20}$ .