

# Homework 4

Math 262

recommended completion date: Monday, October 10

You should do these problems for your own practice, but *your solutions will not be collected or graded*. Solutions are posted on Moodle so you can check your own work.

## Book Problems

- Section 2.3 #47 (page 94)
- Section 2.4 #49, 50, 52, 58, 66, 71 (pages 102–106)
- Section 2.5 #75, 77 (pages 111–112)

## Additional Problems

1. A total of  $n$  independent tosses of a coin that lands on heads with probability  $p$  are made. How large need  $n$  be so that the probability of obtaining at least one head is at least  $\frac{1}{2}$ ? (The answer depends on  $p$ , of course.)
2. A pair of dice is rolled until a sum of either 5 or 7 appears. Find the probability that 5 occurs first. *Hint*: One way to do this is to let  $E_n$  be the event that a 5 occurs on the  $n^{\text{th}}$  roll and no 5 or 7 occurs on the first  $n - 1$  rolls. Compute  $P(E_n)$  and argue that  $\sum_{n=1}^{\infty} P(E_n)$  is the desired probability.