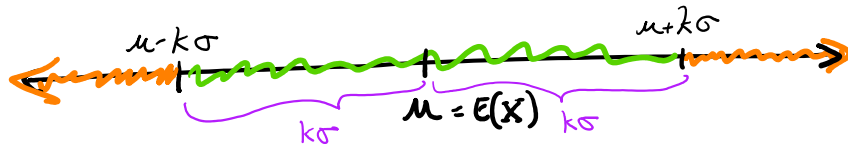


**Chebyshev's Inequality:** Let  $X$  be a discrete random variable with mean  $\mu$  and standard deviation  $\sigma$ . For any  $k \geq 1$ ,

$$P(|X - \mu| \geq k\sigma) \leq \frac{1}{k^2}.$$

In words, the probability that  $X$  is at least  $k$  standard deviations away from its mean is at most  $\frac{1}{k^2}$ .



$$P(X \text{ is in orange shaded region}) \leq \frac{1}{k^2}$$

$$P(X \text{ is in green shaded region}) \geq 1 - \frac{1}{k^2}$$

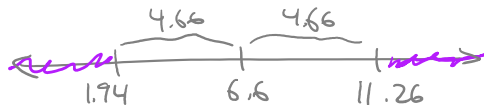
②

$$P(|X - \mu| \geq k\sigma) \leq \frac{1}{k^2}$$

$$\mu = 6.6 \quad k = 2 \quad \sigma = \sqrt{5.44} = 2.33$$

$$P(|X - 6.6| \geq 2(2.33)) = P(|X - 6.6| \geq 4.66)$$

$$= P(X \leq 6.6 - 4.66 \text{ or } X \geq 6.6 + 4.66)$$



$$= P(X \leq 1.94 \text{ or } X \geq 11.26)$$

not possible                      not possible for this  $X$

$$= 0, \text{ which is less than } \frac{1}{k^2} = \frac{1}{4}$$

so Chebyshev's inequality holds